

NAME

`y0`, `y0f`, `y0l`, `y1`, `y1f`, `y1l`, `yn`, `ynf`, `ynl` - Bessel functions of the second kind

SYNOPSIS

```
#include <math.h>
```

```
double y0(double x);
double y1(double x);
double yn(int n, double x);
```

```
float y0f(float x);
float y1f(float x);
float ynf(int n, float x);
```

```
long double y0l(long double x);
long double y1l(long double x);
long double ynl(int n, long double x);
```

Link with `-lm`.

Feature Test Macro Requirements for glibc (see [feature_test_macros\(7\)](#)):

`y0()`, `y1()`, `yn()`:

```
_XOPEN_SOURCE || /* Since glibc 2.19: */ _DEFAULT_SOURCE || /* Glibc versions <= 2.19: */
_SVID_SOURCE || _BSD_SOURCE
```

`y0f()`, `y0l()`, `y1f()`, `y1l()`, `ynf()`, `ynl()`:

```
_XOPEN_SOURCE >= 600 || (_ISOC99_SOURCE && _XOPEN_SOURCE) || /* Since glibc 2.19:
*/ _DEFAULT_SOURCE || /* Glibc versions <= 2.19: */ _SVID_SOURCE || _BSD_SOURCE
```

DESCRIPTION

The `y0()` and `y1()` functions return Bessel functions of x of the second kind of orders 0 and 1, respectively. The `yn()` function returns the Bessel function of x of the second kind of order n .

The value of x must be positive.

The `y0f()`, `y1f()`, and `ynf()` functions are versions that take and return *float* values. The `y0l()`, `y1l()`, and `ynl()` functions are versions that take and return *long double* values.

RETURN VALUE

On success, these functions return the appropriate Bessel value of the second kind for x .

If x is a NaN, a NaN is returned.

If x is negative, a domain error occurs, and the functions return `-HUGE_VAL`, `-HUGE_VALF`, or `-HUGE_VALL`, respectively. (POSIX.1-2001 also allows a NaN return for this case.)

If x is 0.0, a pole error occurs, and the functions return `-HUGE_VAL`, `-HUGE_VALF`, or `-HUGE_VALL`, respectively.

If the result underflows, a range error occurs, and the functions return 0.0

If the result overflows, a range error occurs, and the functions return `-HUGE_VAL`, `-HUGE_VALF`, or `-HUGE_VALL`, respectively. (POSIX.1-2001 also allows a 0.0 return for this case.)

ERRORS

See [math_error\(7\)](#) for information on how to determine whether an error has occurred when calling these functions.

The following errors can occur:

Domain error: x is negative

`errno` is set to `EDOM`. An invalid floating-point exception (`FE_INVALID`) is raised.

Pole error: x is 0.0

errno is set to **ERANGE** (but see **BUGS**). No **FE_DIVBYZERO** exception is returned by `fetestexcept(3)` for this case.

Range error: result underflow

errno is set to **ERANGE**. No **FE_UNDERFLOW** exception is returned by `fetestexcept(3)` for this case.

Range error: result overflow

errno is not set for this case. An overflow floating-point exception (**FE_OVERFLOW**) is raised.

ATTRIBUTES

For an explanation of the terms used in this section, see `attributes(7)`.

| Interface | Attribute | Value |
|---|---------------|---------|
| y0() , y0f() , y0l() | Thread safety | MT-Safe |
| y1() , y1f() , y1l() | Thread safety | MT-Safe |
| yn() , ynf() , ynl() | Thread safety | MT-Safe |

CONFORMING TO

The functions returning *double* conform to SVr4, 4.3BSD, POSIX.1-2001, POSIX.1-2008. The others are nonstandard functions that also exist on the BSDs.

BUGS

On a pole error, these functions set *errno* to **EDOM**, instead of **ERANGE** as POSIX.1-2004 requires.

In glibc version 2.3.2 and earlier, these functions do not raise an invalid floating-point exception (**FE_INVALID**) when a domain error occurs.

SEE ALSO

`j0(3)`

COLOPHON

This page is part of release 4.10 of the Linux *man-pages* project. A description of the project, information about reporting bugs, and the latest version of this page, can be found at <https://www.kernel.org/doc/man-pages/>.